**IMPORTANT NOTICE – Mandatory Requirement to Report**

This course will be conducted using remote instruction. Students who are accessing the course from outside of Canada or the USA must notify the instructor and indicate in which country they are located. Access to software may be restricted from some countries and failure to comply with these restrictions may result in criminal prosecution.

**Course Objectives**

To study the mathematical formulation and apply numerical techniques to the solution of practical problems encountered in electrical and computer engineering. Applications include circuit, transmission-line, and electromagnetic field modelling, both in the frequency and the time domain. Mathematical formulations include linear and non-linear systems of equations, linear and non-linear systems of ordinary differential equations, systems of partial differential equations, and integral equations. Optimization problems will be studied both as alternative mathematical formulations of the modelling problem as well as for design. Numerical discretization methods to be studied include finite differences, finite element and boundary element methods, as well as the Method of Moments.

**Course Content**

The following topics will be covered:

- Circuit modelling (frequency and time domain solutions).
- Formal methods of formulating circuit equations – KCL, KVL, Modified Nodal Analysis (MNA).
- Methods of solving systems of ODEs.
- Multiconductor transmission-line (MTL) modelling.
- Finite-difference solution of MTL equations.
- Finite-differences for electrostatic and magnetostatic problems.
- Laplace’s equation and PUL matrices of MTLs.
- Iterative matrix solution techniques (Successive-Over-Relaxation, conjugate-gradient).
- Finite Element Method.
- Variational method and development of functionals for PDE’s.
- FEM for the Laplace and Helmholtz equations.
- Grid generation using Gmesh.
- Finite-Difference Time-Domain solution of Maxwell’s equations.
- 2D and 3D, scattered and total field formulations.
- Absorbing boundary conditions.
- Method of Moments (MoM)
  - Green’s function.
  - Green’s theorem.
  - MoM solution of capacitance extraction problem.

**Other Resources**


**Academic Integrity**

Students are expected to conduct themselves in accordance with the highest ethical standards of the Profession of Engineering and evince academic integrity in all their pursuits and activities at the university. As such, in accordance with the General Academic Regulations on Academic Integrity, students are reminded that plagiarism or any other form of cheating in examinations, term tests, assignments, projects, or laboratory reports is subject to serious academic penalty (e.g. suspension or expulsion from the faculty or university). A student found guilty of contributing to cheating by another student is also subject to serious academic penalty.
Learning Outcomes

1. Ability to formulate any circuit problem in a form amenable to computer solution and solve using appropriate numerical analysis procedure.
2. Ability to formulate electromagnetic field problem using either integral equations or PDEs.
3. Ability to discretize an electromagnetic field problem using finite-differences, finite-elements, and the method of moments and program its solution on a computer.
4. Interpret the numerical solutions to extract typical engineering parameters.
5. Ability to analyze stability of numerical procedures for ODEs and particular PDEs.

Expected Competency Levels

<table>
<thead>
<tr>
<th>Outcome</th>
<th>KB</th>
<th>PA</th>
<th>IN</th>
<th>DE</th>
<th>ET</th>
<th>IT</th>
<th>CS</th>
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Evaluation

The final course grade will be determined from a student’s performance on projects, in laboratory quizzes, and on the final examination. Students must complete all the laboratories and projects in order to be eligible to receive a passing grade.

<table>
<thead>
<tr>
<th>Component</th>
<th>Value (%)</th>
<th>Method of Feedback</th>
<th>Learning Outcomes Evaluated</th>
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<tr>
<td>Assignments</td>
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<td>F, S</td>
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<td>Laboratories</td>
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<td>Final Examination</td>
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* Method of Feedback: F - Formative (written comments and/or oral discussion), S - summative (numerical grade)

CEAB Graduate Attributes Assessed

KB.4 – Recalls and defines, and/or comprehends and applies, first principles and concepts in specialized engineering science.

IN.3 – Interprets results and reaches appropriate conclusions.

Requirements and Regulations

- Attendance at lectures and laboratories is essential for successful completion of this course. Students must satisfy each evaluation component in the course to receive a final grade.
- It is the responsibility of each student to contact the instructor in a timely manner if he or she is uncertain about his or her standing in the course and about his or her potential for receiving a failing grade. Students should also familiarize themselves with the University’s General Academic Regulations, as well as Section 3 of the Faculty of Engineering Academic Regulations dealing with incomplete term work, deferred examinations, attendance and withdrawal.
- No programmable devices or systems (such as calculators, PDAs, iPods, iPads, cell phones, wireless communication or data storage devices) are allowed in examinations unless approved by the course instructor.
- Students should be aware that they have access to an extensive range of resources and support organizations. These include Academic Resources, Counselling, Advocacy and Accessibility Offices as well as documentation of key University policies e.g. Academic Integrity, Respectful Behaviour, Examinations and related matters.

Supplemental Information
Copyright Notice
All materials provided in this course are copyright and are provided under the fair dealing provision of the Canadian Copyright Act. This material may not be redistributed in any manner without the express written permission of the relevant copyright holder.

Retention of Student Work
Students are advised that copies of their work submitted in completing course requirements (i.e. assignments, laboratory reports, project reports, test papers, examination papers, etc.) may be retained by the instructor and/or the department for the purpose of student assessment and grading, and to support the ongoing accreditation of each Engineering program. This material shall be handled in accordance with the University's Intellectual Property Policy and the protection of privacy provisions of The Freedom of Information and Protection of Privacy Act (Manitoba). Students who do not wish to have their work retained must inform the Head of Department, in writing, at their earliest opportunity.